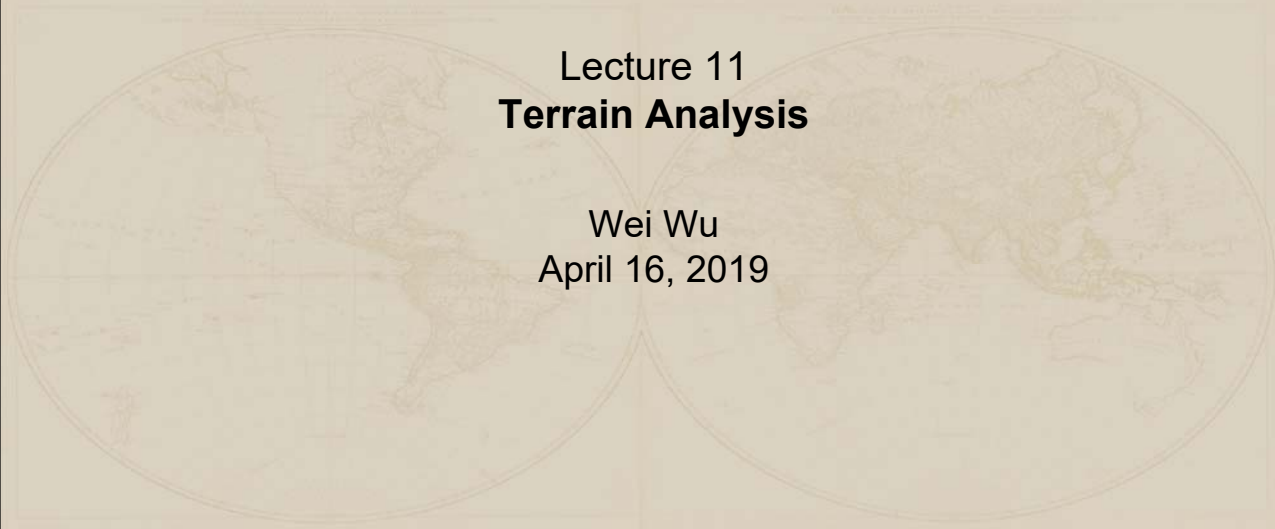


COA 690/790 GIS in Marine Science

The background of the slide is a light beige color with a faint, stylized world map. The map is centered on the Atlantic Ocean, showing the continents of North and South America on the left and Europe and Africa on the right. The map is composed of two circular hemispheres joined at the equator.

## Lecture 11 Terrain Analysis

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April 16, 2019

### Digital Elevation Models

Terrain determines the natural availability and location of surface water, and hence soil moisture and drainage.

Terrain affects water quality through control of sediment generation and transport.

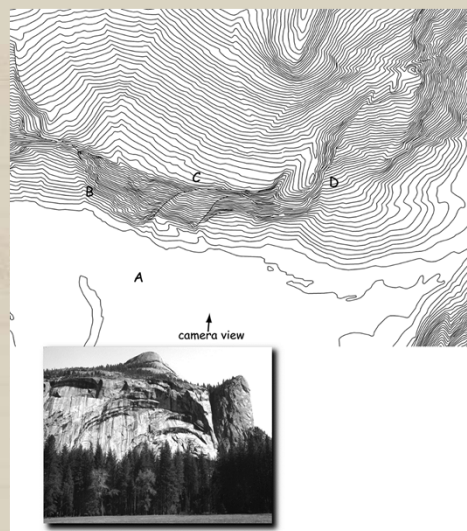
Elevation, slope steepness and direction defines flood zones, watershed boundaries and hydrologic networks.

Terrain also strongly influences location and nature of transportation networks or the cost and methods of house and road construction.

**Table 11-1:** A subset of commonly used terrain variables. (adapted from Moore et al., 1993).

Variable	Description	Importance
Height	Elevation above base	Temperature, vegetation, visibility
Slope	Rise relative to horizontal distance	Water flow, flooding, erosion, travel cost, construction suitability, geology, insolation, soil depth
Aspect	Downhill direction of steepest slope	Insolation, temperature, vegetation, soil characteristics and moisture, visibility
Upslope area	Watershed area above a point	Soil moisture, water runoff volume and timing, pollution or erosion hazards
Flow length	Longest upstream flow path to a point	Sediment and erosion rates
Upslope length	Mean upstream flow path length to a point	Sediment and erosion rates
Profile curvature	Curvature parallel to slope direction	Erosion, water flow acceleration
Plan curvature	Curvature perpendicular to slope direction	Water flow convergence, soil water, erosion
Visibility	Site obstruction from given view-points	Utility location, watershed preservation

## Contour lines (Topographic contours)



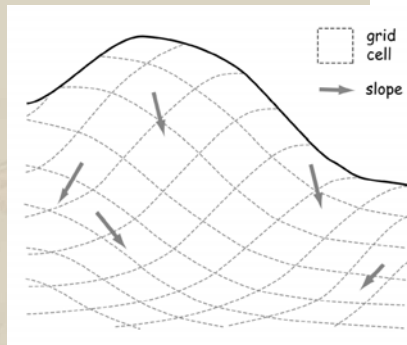
Most terrain analysis are performed using a raster data model

### Digital Elevation Models

#### Terrain Analysis - Slope and Aspect

- Used for: hydrology, conservation, site planning, other infrastructure development.
- Watershed boundaries, flowpaths and direction, erosion modeling, and viewshed determination all use slope and/or aspect data as input.
- Slope is defined as the change in elevation (*a rise*) with a change in horizontal position (*a run*).
- Slope is often reported in degrees (*0° is flat, 90° is vertical*)

#### Slope (continued)

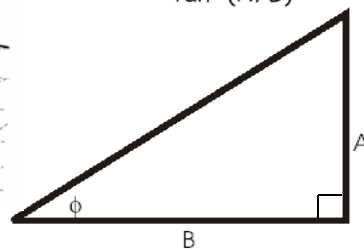


$$\text{Slope as Percent} = \frac{\text{rise}}{\text{run}} * 100$$

$$= A/B * 100$$

$$\text{Slope as Degrees} = \phi$$

$$= \tan^{-1}(A/B)$$



To convert from percent slope to degrees, apply formula,  
e.g. 3% = how many degrees?

$$A/B * 100 = 3, \text{ then } A/B = 3/100 = 0.03$$

$$= \tan^{-1}(0.03) = 1.72 \text{ degrees}$$

**Slope (continued)**

Measured in the steepest direction of elevation change

Often does not fall parallel to the raster rows or columns

Which cells to use?

Several different methods:

- Four nearest cells
- 3<sup>rd</sup> Order Finite Difference

42	45	47
40	44	49
44	48	52

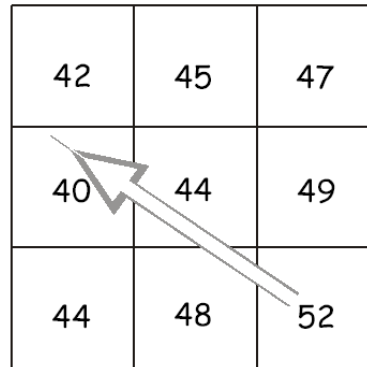


Figure 11-18: Direction of steepest slope.

**Slope (continued)**

Elevation is Z

- Using a 3 by 3 (or 5 by 5) moving window
- Each cell is assigned a subscript and the elevation value at that location is referred to by a subscripted Z value

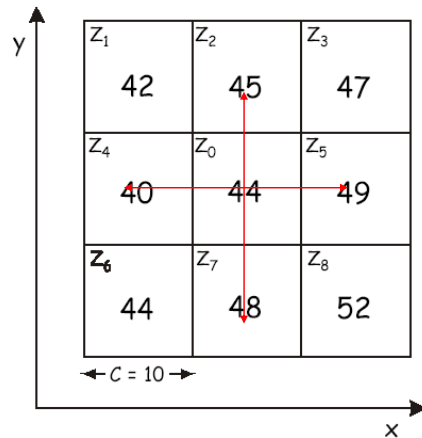
The most common formula:

$$s = \text{atan} \sqrt{\left(\frac{dZ}{dx}\right)^2 + \left(\frac{dZ}{dy}\right)^2}$$

Slope (continued)

$$dZ/dx = (Z_5 - Z_4)/(2C)$$

$$dZ/dy = (Z_2 - Z_7)/(2C)$$



for  $Z_0$

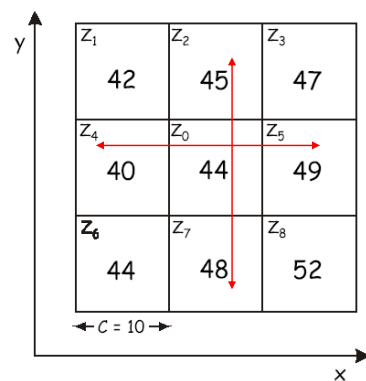
$$\Delta Z/\Delta x = (49 - 40)/20 = 0.45$$

$$\Delta Z/\Delta y = (45 - 48)/20 = -0.15$$

$$\text{slope} = \tan^{-1} [(0.45)^2 + (-0.15)^2]^{1/2}$$

$$= 25.3^\circ$$

Slope (continued)



Generalized formula for

 $\Delta Z/\Delta x$  and  $\Delta Z/\Delta y$ 

$$\Delta Z/\Delta x = (Z_5 - Z_4)2^*$$

$$\Delta Z/\Delta y = (Z_2 - Z_7)2^*$$

\* = times cell width

Using the four nearest cells

- Slope calculation base on cells adjacent to the center cell
- The distance is from cell center to cell center

## Slope (continued)

**Multiply** (kernel, cell by cell)

**Add** (results)

**Divide by #cells x cell width**

**Use slope formula**

Four nearest cells  
elevation values

42	45	47
40	44	49
44	48	52

← C = 10 →

Kernel for  $\Delta Z/\Delta x$  |x

$Z_1$	$Z_2$	$Z_3$
0	0	0
$Z_4$	$Z_0$	$Z_5$
-1	0	1
$Z_6$	$Z_7$	$Z_8$
0	0	0

$$\Delta Z/\Delta x = (49 - 40)/20 = 0.45 \quad .5$$

Kernel for  $\Delta Z/\Delta y$  |y

$Z_1$	$Z_2$	$Z_3$
0	1	0
$Z_4$	$Z_0$	$Z_5$
0	0	0
$Z_6$	$Z_7$	$Z_8$
0	-1	0

$$\Delta Z/\Delta y = (45 - 48)/20 = -0.15 \quad .5$$

$$\text{slope} = \tan^{-1} [(0.45)^2 + (-0.15)^2]^{0.5}$$

$$\text{slope} = 25.3^\circ$$

3rd-order Finite Difference  
elevation values

42	45	47
40	44	49
44	48	52

← C = 10 →

kernel for  $dZ/dx$

$Z_1$	$Z_2$	$Z_3$
-1	0	1
$Z_4$	$Z_0$	$Z_5$
-2	0	2
$Z_6$	$Z_7$	$Z_8$
-1	0	1

$$dZ/dx = [1 * (47 - 42) + 2 * (49 - 40) + 1 * (52 - 44)] / 80 = 0.39$$

kernel for  $dZ/dy$

$Z_1$	$Z_2$	$Z_3$
1	2	1
$Z_4$	$Z_0$	$Z_5$
0	0	0
$Z_6$	$Z_7$	$Z_8$
-1	-2	-1

$$dZ/dy = [1 * (47 - 52) + 2 * (45 - 48) + 1 * (42 - 44)] / 80 = -0.16$$

$$\text{slope} = \tan^{-1} [(0.39)^2 + (-0.16)^2]^{0.5}$$

$$\text{slope} = 22.9^\circ$$

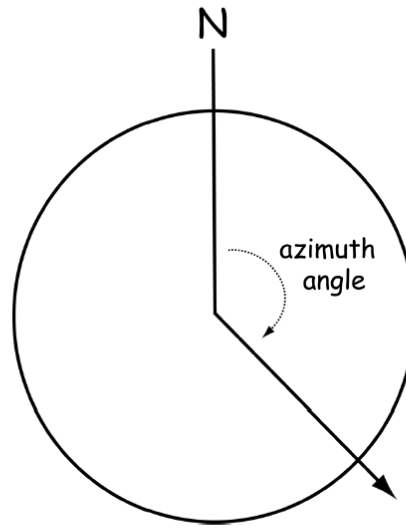
**Multiply** (kernel, cell by cell)

**Add** (results)

**Divide by #cells x cell width**

**Use slope formula**

## Aspect



**Figure 11-7:** Aspect may be reported as an azimuth angle, measured clockwise in degrees from north.

## Aspect

The orientation (*in compass angles*) of a slope

Calculation:

$$\text{Aspect} = \tan^{-1} [ -(\Delta Z / \Delta y) / (\Delta Z / \Delta x) ]$$

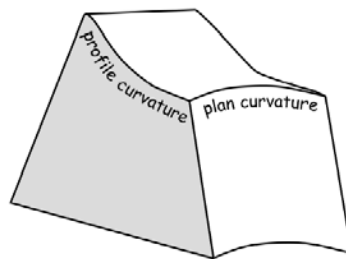
As with slope, estimated aspect varies with the methods used to determine  $\Delta Z / \Delta x$  and  $\Delta Z / \Delta y$

Aspect calculations also use the four nearest cell or the 3<sup>rd</sup>-order finite difference methods

## Curvature

$Z_1$	$Z_2$	$Z_3$
$Z_4$	$Z_0$	$Z_5$
$Z_6$	$Z_7$	$Z_8$

←  $C$  →



$$D = [(Z_4 + Z_5)/2 - Z_0] / C^2$$

$$E = [(Z_2 + Z_7)/2 - Z_0] / C^2$$

$$F = (Z_3 - Z_1 + Z_6 - Z_8) / 4C^2$$

$$G = (Z_5 - Z_4) / 2C$$

$$H = (Z_2 - Z_7) / 2C$$

plan curvature

$$\frac{2 (bH^2 + EG^2 - FGH)}{G^2 + H^2}$$

profile curvature

$$\frac{-2 (DG^2 + EH^2 + FGH)}{G^2 + H^2}$$

## Flow direction

Use in hydrologic analysis

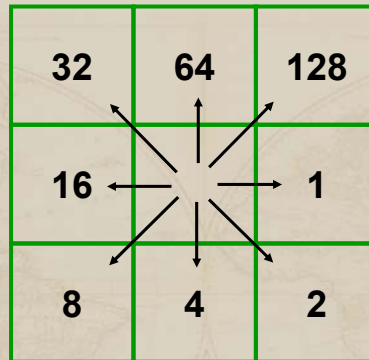
Excess water at a point on the Earth will flow in a given direction

Flow may be either on or below surface but always in the direction of steepest descent (often the same as local aspect)

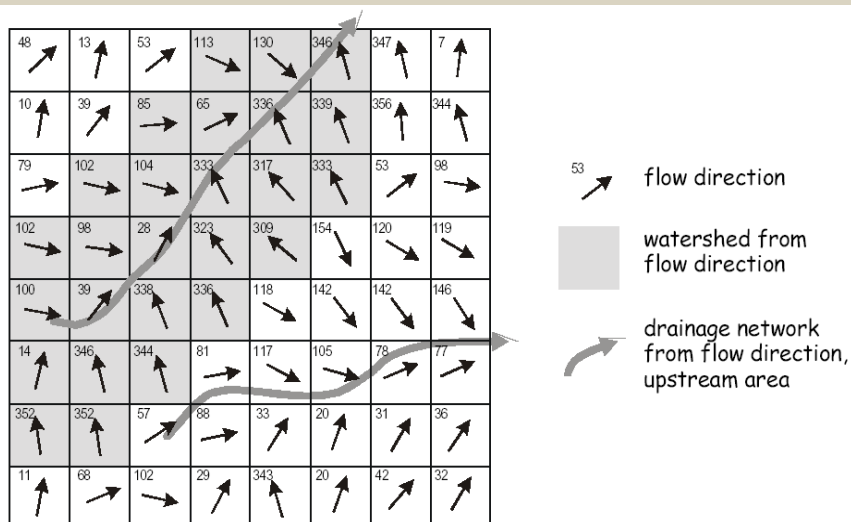
Directions stored as compass angle in raster data layer



## Eight Direction Pour Point Model



ESRI Direction encoding



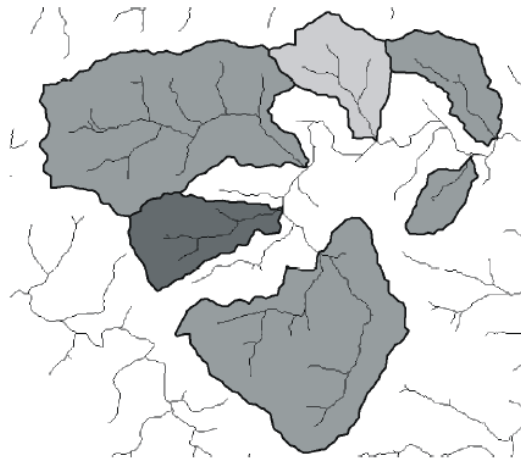
**Figure 11-21:** Flow direction, watershed, and drainage network shown for a raster grid. Elevation data are used to define the flow direction for each cell. These flow directions are then used to determine a number of important hydrologic functions.

## Watershed

- An area that contributes flow to a point on the landscape  
*Water falling anywhere in the upstream area of a watershed will pass through that point.*
- Many be small or large
- Identified from a flow direction surface

## Drainage network

- A set of cells through which surface water flows
- Based on the flow direction surface



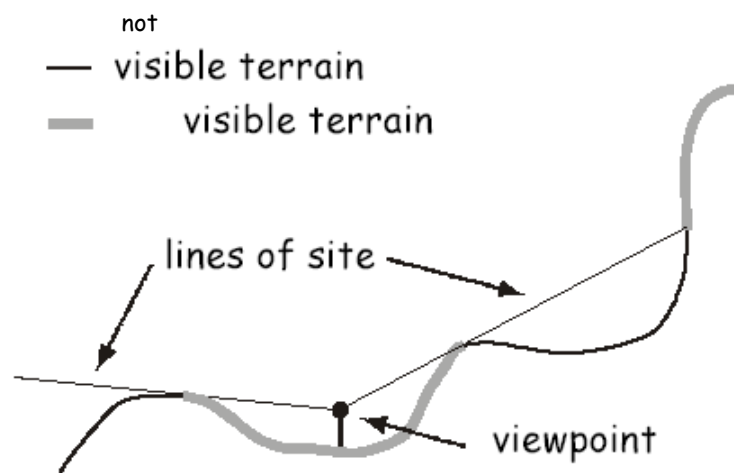
**Figure 11-22:** Drainage network and watersheds derived from DEM. Flow direction was determined from local aspect. Upstream watersheds and the probably drainage paths were then determined from flow direction.

## Viewshed

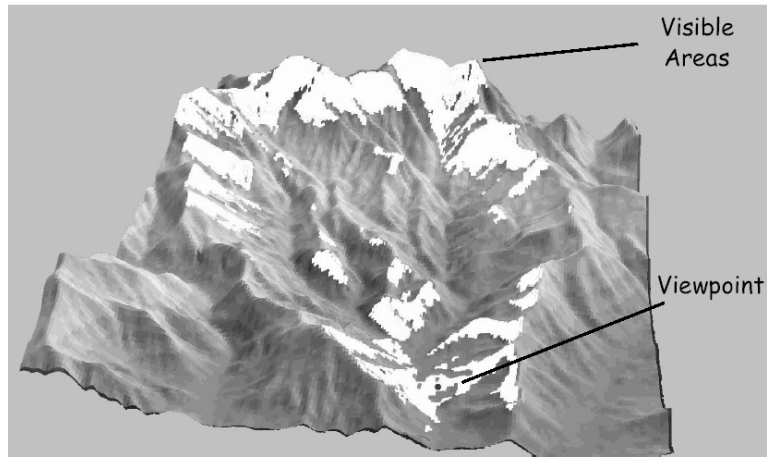
The *viewshed* for a point is the collection of areas visible from that point.

Views from any non-flat location are blocked by terrain.

Elevations will hide a point if they are higher than the viewing point, or higher than the line of site between the viewing point and target point

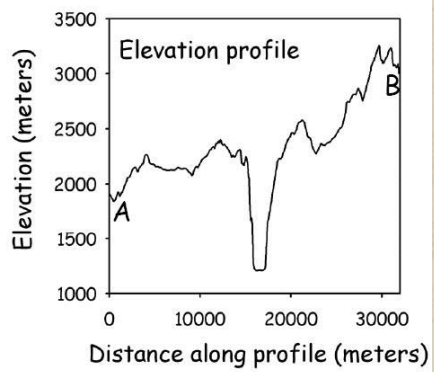
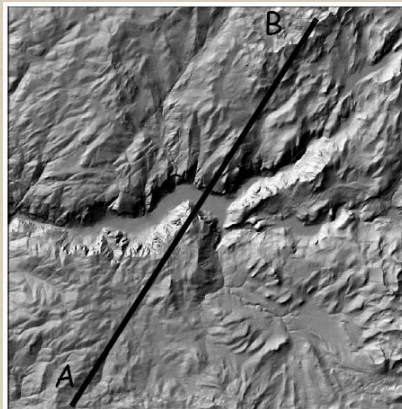


**Figure 11-23:** Mechanics of defining a viewshed

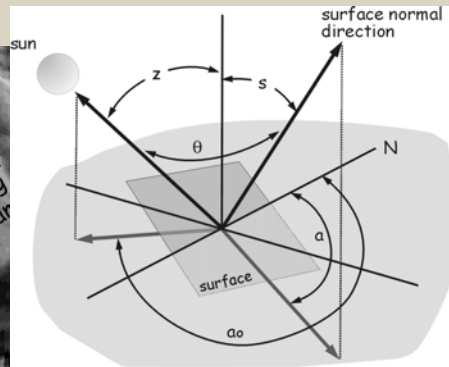
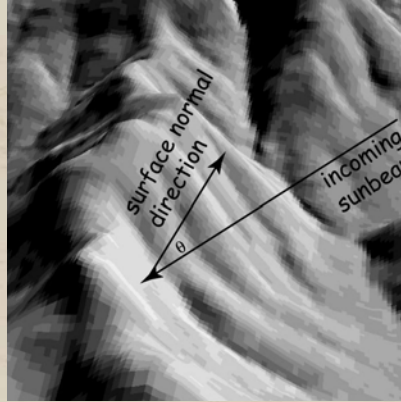


**Figure 11-24:** An example of a viewpoint, and corresponding viewedshed.

## Profile plots



## Shaded Relief Surfaces



incidence angle  $\theta$  is equal to:  
 $\cos^{-1}[\cos(z)\cos(s) + \sin(z)\sin(s)\cos(\alpha_0 - a)]$   
 where:  $z$  is the solar zenith angle  
 $\alpha_0$  is the solar azimuth angle  
 $s$  is the surface normal slope angle  
 $a$  is the surface normal azimuth angle